



Estd 2009

Shri Balasaheb Mane Shikshan Prasarak Mandal's  
**ASHOKRAO MANE GROUP OF INSTITUTIONS**

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**Approved by :** AICTE, New Delhi No. F-No. MS ( NewInt ) 2009 / 08, Higher & Technical Education Department, Govt. of Maharashtra, Directorate of Technical Education, Mumbai. **Affiliated to :** Dr. Babasaheb Ambedkar Technological University, Lonere - Raigad. (B.Tech. & M.Tech. Programs), Shivaji University, Kolhapur. (MBA Program).

**Accredited by NAAC**

**Founder President**

**Late Shri. Ashokrao Mane**

**Director**

**Dr. A. V.Deshmukh**, M.E., Ph.D.

**President**

**Hon. Shri. Vijaysinh A. Mane**

Ref. No. :

Date :

**Criteria 2 :TEACHING-LEARNING AND EVALUATION**

**Summary Sheet**

**2.5 - Evaluation Process and Reforms**

2.5.1 - Mechanism of internal assessment is transparent and robust in terms of frequency and mode.

Sr. No.	Content
1	Sample Documents of Continuous Assessment-I (CA-I), Mid Semester Examination (MSE) and Continuous Assessment-II (CA-II) Examinations - <ul style="list-style-type: none"> <li>• Exam Time Table</li> <li>• Question Papers</li> <li>• Model Answers</li> <li>• Marksheet</li> <li>• One sample of Evaluated Answer Sheet</li> </ul>



ASHOKRAO MANE GROUP OF INSTITUTIONS, VATHAR.

Faculty of Engineering

## CIRCULAR/NOTICE

Doc. No.: AMGOI -FRM-03

Rev. No.: 00

Rev. Dt: 04/07/2013

Date-04/09/2023

All the students are hereby informed that, departmental **CA-1** Semester Exam is scheduled from **14/09/2023** to **15/09/2023** of **20 marks**. The details of the schedule are as follows.

DATE	TIME	SY	TY	B.Tech
14/09/2023	10.15.am to 11.15am	M III	EFT	ME
14/09/2023	12.30pm to 01.30pm	EDC	DSP	FOC
14/09/2023	02.30pm to 03.30pm	-	ACOM	MCOM
15/ 09/2023	10.15.am to 11.15am	DE <i>Patil</i>	AC	ED
15/ 09/2023	12.30pm to 01.30pm	EMI	CSE	EEFM

*S.A.*  
Mr. S. A. Bhosale  
Exam coordinator



*S.S.*  
Mrs. S. S. Patil  
H.O.D

**DR. BABASAHEBAMBEDKAR TECHNOLOGICAL UNIVERSITY, LONERE**

Continuous Assessment I – Nov., 2021

Course: B. Tech in Electronics & Telecommunication Engineering

Sem: V

Subject Name: Digital Signal Processing

Subject Code: BTETC502

Max Marks: 20

Date: 14/09/2023

Duration: 1 Hr.

**Instructions to the Students:**

1. Solve all questions .
2. Assume suitable data if required.
3. Use of non-programmable scientific calculator is allowed.

		(Level/CO)	Marks
		<b>05*01M</b>	
<b>Q. 1</b>	<b>Fill in the blank</b>		
A.	_____ is done to convert a continuous-time signal into discrete-time signal.	R/BTETC502.1	<b>01</b>
B.	Sampling frequency of the signal $x(t)=\sin(200\pi t)+\cos(400\pi t)$ is _____	Ap/BTETC502.1	<b>01</b>
C.	If $X(k)$ discrete Fourier transform of $x(n)$ , then the inverse discrete Fourier transform of $X(k) =$ _____	R/BTETC502.1	<b>01</b>
D.	_____ Complex multiplications and _____ complex additions requires for computing an N-point DFT.	R/BTETC502.1	<b>01</b>
E.	The $N^{\text{th}}$ root of unity $W_N$ is given as _____	R/BTETC502.1	<b>01</b>
		<b>03*05 M</b>	
<b>Q.2</b>	<b>Solve any Three of the following.</b>		
A.	Explain Advantages of Digital over Analog signal processing	U/BTETC502.2	<b>05</b>
B.	Find the DTFT of an exponential sequence: $x[n] = a^n u[n]$ where $ a  < 1$	Ap/BTETC502.2	<b>05</b>
C.	Determine 4 point DFT of a signal $x(n)=\{1, 1\}$ using standard formula and sketch its magnitude & Phase.	An/BTETC502.2	<b>05</b>
D.	Define Twiddle Factor. Explain Properties of twiddle factor & compute the DFT of 4 point sequence $x(n)=\{0,1, 2, 3\}$ using matrix form.	Ap/BTETC502.1	<b>05</b>

**DR. BABASAHEBAMBEDKAR TECHNOLOGICAL UNIVERSITY, LONERE**

**Continuous Assessment I – Nov., 2021**

Course: **B. Tech in Electronics & Telecommunication Engineering** Sem: **V**

Subject Name: **Digital Signal Processing**

Subject Code: **BTETC502**

Max Marks: **20**

Date: **14/09/2023**

Duration: **1 Hr.**

		(Level/CO)	Marks
<b>Q. 1</b>	<b>Fill in the blank</b>	<b>05*01M</b>	
A.	<u>Sampling</u> is done to convert a continuous-time signal into discrete-time signal.	R/BTETC502.1	<b>01</b>
B.	Sampling frequency of the signal $x(t)=\sin(200\pi t)+\cos(400\pi t)$ is <u>400Hz</u>	Ap/BTETC502.1	<b>01</b>
C.	If $X(k)$ discrete Fourier transform of $x(n)$ , then the inverse discrete Fourier transform of $X(k) = \frac{1}{N} \sum_{k=0}^{N-1} X(k) e^{\frac{j2\pi nk}{N}}$ for $n=0,1,2,\dots,N-1$	R/BTETC502.1	<b>01</b>
D.	$N^2$ Complex multiplications and $N(N-1)$ complex additions requires for computing an $N$ -point DFT.	R/BTETC502.1	<b>01</b>
E.	The $N^{\text{th}}$ root of unity $W_N$ is given as $e^{-\frac{j2\pi}{N}}$	RBTETC502.1	<b>01</b>
<b>Q.2</b>	<b>Solve any Three of the following.</b>	<b>03*05 M</b>	
A.	<p>Explain Advantages of Digital over Analog signal processing</p> <ol style="list-style-type: none"> <li><b>Flexibility and Versatility:</b> Digital signals can be easily manipulated using software, allowing for versatile processing. Algorithms can be altered or updated without changing the hardware, providing flexibility in adapting to different requirements.</li> <li><b>Precision and Accuracy:</b> Digital processing allows for high precision and accuracy in signal manipulation. Digital systems are less susceptible to noise and distortion compared to analog systems, enabling more reliable and consistent results.</li> <li><b>Signal Preservation:</b> Digital signals can be copied and transmitted without degradation, whereas analog signals tend to degrade with each copy or transmission due to noise and interference.</li> <li><b>Ease of Storage and Transmission:</b> Digital signals can be stored efficiently and transmitted over long distances without significant loss of quality. Compression techniques can be applied to reduce file sizes without compromising signal quality, making storage and transmission more efficient.</li> <li><b>Cost-Effectiveness:</b> While initial setup costs for digital systems might be higher due to hardware and software requirements, they often become more cost-effective in the long run. Digital technology benefits from economies of scale and ongoing improvements in manufacturing processes, making it more affordable over time.</li> <li><b>Complex Processing Capabilities:</b> Digital processing enables complex algorithms and computations that might be impractical or impossible in analog systems. This capability is particularly valuable in applications such as image processing, data analysis, and communications.</li> <li><b>Ease of Integration:</b> Digital systems can be easily integrated with other digital devices and systems, facilitating compatibility and interoperability across a wide range of technologies.</li> <li><b>Ease of Modification and Upgrade:</b> Digital systems can be modified or upgraded through software changes, avoiding the need for extensive hardware alterations. This ease of upgrade can extend the lifespan of devices and systems.</li> </ol> <p align="right">----(each 1 of 1M)</p>	U/BTETC502.2	<b>05</b>



B.	<p>Find the DTFT of an exponential sequence: <math>x[n] = a^n u[n]</math> where <math> a  &lt; 1</math></p> $X(\omega) = DTFT \{x[n]\} = \sum_{n=-\infty}^{\infty} x[n] e^{-j\omega n}$ <p>Given signal is, <math>x[n] = \alpha^n u[n]</math></p> $X(\omega) = \sum_{n=-\infty}^{\infty} \alpha^n u[n] e^{-j\omega n}$ $= \sum_{n=0}^{\infty} (\alpha e^{-j\omega})^n$ $= \frac{1}{1 - \alpha e^{-j\omega}}$ <p style="text-align: right;">---(each step 1M)</p>	Ap/BTETC502.2	05
C.	<p>Determine 4 point DFT of a signal <math>x(n) = \{1, 1\}</math> using standard formula and sketch its magnitude &amp; Phase.</p> <p>Let us assume <math>N = L = 4</math>.</p> <p>We have <math>X(k) = \sum_{n=0}^{N-1} x(n) e^{-j2\pi nk/N} \quad k = 0, 1, \dots, N - 1</math></p> $X(0) = \sum_{n=0}^3 x(n) = x(0) + x(1) + x(2) + x(3)$ $= 1 + 1 + 0 + 0 = 2$ $X(1) = \sum_{n=0}^3 x(n) e^{-j\pi n/2} = x(0) + x(1) e^{-j\pi/2} + x(2) e^{-j\pi} + x(3) e^{-j3\pi/2}$ $= 1 + \cos \frac{\pi}{2} - j \sin \frac{\pi}{2}$ $= 1 - j$ $X(2) = \sum_{n=0}^3 x(n) e^{-j\pi n} = x(0) + x(1) e^{-j\pi} + x(2) e^{-j2\pi} + x(3) e^{-j3\pi}$ $= 1 + \cos \pi - j \sin \pi$ $= 1 - 1 = 0$ $X(3) = \sum_{n=0}^3 x(n) e^{-j3\pi n/2} = x(0) + x(1) e^{-j3\pi/2} + x(2) e^{-j3\pi} + x(3) e^{-j9\pi/2}$ $= 1 + \cos \frac{3\pi}{2} - j \sin \frac{3\pi}{2}$ $= 1 + j$ $X(k) = \{2, 1 - j, 0, 1 + j\}$ <p style="text-align: right;">---(each step 1M)</p>	An/BTETC502.2	05

D. Define Twiddle Factor. Explain Properties of twiddle factor & compute the DFT of 4 point sequence  $x(n)=\{0,1, 2, 3\}$  using matrix form.

**Twiddle Factor**

It is denoted as  $W_N$  and defined as  $W_N = e^{-j2\pi/N}$ . Its magnitude is always maintained at unity. Phase of  $W_N = -2\pi/N$ . It is a vector on unit circle and is used for computational convenience. Mathematically, it can be shown as -

$$W_N^r = W_N^{r\pm N} = W_N^{r\pm 2N} = \dots \quad \text{---(1M)}$$

1.  $W_N^{k+\frac{N}{2}} = e^{-\frac{j2\pi k}{N}} e^{-j\pi} = -W_N^k$  (Symmetry Property)

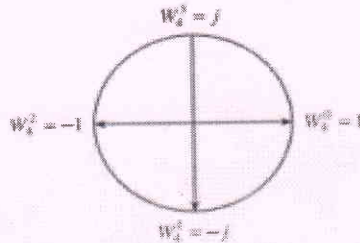
2.  $W_N^{k+N} = e^{-\frac{j2\pi k}{N}} e^{-j2\pi} = W_N^k$  (periodicity property) --(1M)

**Solution** The first step is to determine the matrix  $W_4$ . By exploiting the periodicity property of  $W_4$  and the symmetry property

$$W_N^{k+k/N} = -W_N^k$$

the matrix  $W_4$  may be expressed as

$$W_4 = \begin{bmatrix} W_4^0 & W_4^0 & W_4^0 & W_4^0 \\ W_4^0 & W_4^1 & W_4^2 & W_4^3 \\ W_4^0 & W_4^2 & W_4^4 & W_4^0 \\ W_4^0 & W_4^3 & W_4^0 & W_4^1 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & W_4^1 & W_4^2 & W_4^3 \\ 1 & W_4^2 & W_4^0 & W_4^2 \\ 1 & W_4^3 & W_4^2 & W_4^1 \end{bmatrix}$$



(a) 4-point DFT

$$= \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & -j & -1 & j \\ 1 & -1 & 1 & -1 \\ 1 & j & -1 & -j \end{bmatrix}$$

Then

$$X_4 = W_4 x_4 = \begin{bmatrix} 6 \\ -2 + 2j \\ -2 \\ -2 - 2j \end{bmatrix}$$

---(each step 1M)



Shri Balasaheb Mane Shikshan Prasarak Mandal, Ambap's  
Ashokrao Mane Group of Institutions, Faculty of Engineering  
Vathar Tarf Vadgaon- 416112

Exam: CA-I

Branch: E&TC Engg.

Time: 12-30-1-30

Subject: DSP (Digital Signal Processing)

Date: 14/09/2023

Roll No.	Name of student	Sign	Marks( )
01	Bhosale Dhadyeshik Pratap	<u>Dhadyeshik</u>	03+05=08
02	Chougule Suyog Rajkumar	<u>Suyog</u>	04+04=08
03	Pandurang Namdev Geopane	<u>Namdev</u>	03+06=09
04	Geeta Chandrakant Jagtap	<u>Jagtap</u>	02+10=12
05	Rushikesh Ramesh Kumbhar	<u>Rushikesh</u>	04+06=10
06	Sakshi Sachin Lambe	<u>Lambe</u>	04+09=13
07	Shreyansh Sunil Kininge	<u>Kininge</u>	03+05=08
08	Diksha Dhananjay Mane	<u>Diksha</u>	04+13=17
09	Sakshi Ananda Muthale	<u>Muthale</u>	04+11=15
10	Aditi Raosaheb Patil	<u>Aditi Patil</u>	03+13=16
11	Patil Akhay Dilip	<u>Akhay Patil</u>	05+04=09
12	Aniket Vishwanath Patil	<u>Aniket</u>	04+06=10
13	Ayush Subhash Patil	<u>Ayush Patil</u>	05+05=10
14	Ketan Krushnat Patil	<u>Ketan Patil</u>	04+05=09
15	Pratik Dattatray Patil	<u>Pratik Patil</u>	04+06=10
16	Rohan Shivaji Patil	<u>Rohan Patil</u>	04+04=08
17	Rohini Bharama Patil	<u>Rohini Patil</u>	04+09=13
18	Sakshi Madhukar Patil	<u>Sakshi Patil</u>	04+10=14
19	Patil Vrushabh	<u>Vrushabh Patil</u>	05+04=09
20	Poonita Gbrikant Powar	<u>Poonita</u>	05+05=10
21	Toojakumari N. Rajput	<u>Toojakumari</u>	04+09=13
22	Sonam Kumari N. Rajput	<u>Sonam</u>	04+06=10
23	Ritesh S. Patil	<u>Ritesh Patil</u>	04+12=16
24	Arati Ramchandra Salunkhe	<u>Arati Salunkhe</u>	04+13=17
25	Shubham M. Shinde	<u>Shubham</u>	03+05=08
26	Shirish Y. Shipekar	<u>Shirish</u>	04+04=08
27	Kajal Mohadev Shirke	<u>Kajal Shirke</u>	03+12=15
28	Vaishnavi Vishwas Yadav-Patil	<u>Vaishnavi Patil</u>	03+07=10
29	Prachi Raghunath Yadav	<u>Prachi Yadav</u>	04+08=12
30	Suyash Sanjay Desai	<u>Suyash Desai</u>	04+09=13
31	Pooja M. Powar	<u>Pooja Powar</u>	05+13=18
32	Sardhak Sachin Jadhav	<u>Sardhak Jadhav</u>	03+05=08

Total No. of Present Student: 36

Total No. of Absent Student: 01

Total No. of Student: 37

(D.J. Pawar)  
Jr. Supervisor Name & Sign

Shri Balasaheb Mane Shikshan Prasarak Mandal, Ambap's  
Ashokrao Mane Group of Institutions, Faculty of Engineering  
Vathar Tarf Vadgaon- 416112

Exam:

Branch: E&TC Engg.

Time:

Subject:

Date:

Roll No.	Name of student	Sign	Marks( )
33	Shriya Wayangankar		04+14 = 18
34	Manasi Sannaki	Mgs	02+13 = 15
35	Anjali Patil		03+09 = 12
36	snhejeet. chougule.		03+09 = 12
37	Pathan Umar		Ab
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60			

Total No. of Present Student:

Total No. of Absent Student:

Total No. of Student:

Jr.Supervisor Name & Sign





Q. 2

- A) 1] Digital signal can convey information with less noise, distortion & interference.
- 2] Digital signal can be reproduced easily in mass quantities at comparatively lower cost.
- 3] Digital signal can be easily stored in any magnetic media or optical media using semiconductor chip.
- 4] Digital systems are more accurate and probability of error occurrence can be reduced by employing error detector and corrector codes.
- 5] Digital signal processor is more flexible because DSP operations can be altered using a digitally programmable system.
- 6] Digital signal can be transmitted over long distances.

04

c) Given:  $x(n) = \{1, 1\}$

$x(n) = \{1, 1, 0, 0\} \rightarrow$  Padding  $(N-L)$  zeros in  $x(n)$

$$N = 4, L = 2$$

$$X(k) = \sum_{n=0}^{N-1} x(n) e^{-j2\pi kn/N} \quad k = 0, 1, 2, \dots, N-1$$

$$X(k) = \sum_{n=0}^{N-1} x(n) e^{-j2\pi kn/4} \quad k = 0, 1, 2, 3$$

for  $k=0$

$$X(0) = 1 + 1 + 0 + 0 = 2$$



for  $k=1$

$$x(1) = 1 + e^{-j2\pi(1)/4} + 0 + 0$$
$$= 1 + \cos \pi/2 - j \sin \pi/2$$

$$x(1) = 1 - j$$

for  $k=2$

$$x(2) = 1 + e^{-j2\pi(2)/4}$$
$$= 1 + e^{-j\pi} = 1 - 1$$

$$x(2) = 0$$

for  $k=3$

$$x(3) = 1 + e^{-j2\pi(3)/4}$$
$$= 1 + e^{-j3\pi/2}$$

$$x(3) = 1 + j$$

$$x(n) = \{2, 1-j, 0, 1+j\}$$

$$|x(k)| = \sqrt{(\text{Re})^2 + (\text{Im})^2}$$

$$2 = \sqrt{(2)^2 + (0)^2} = 2$$

$$1-j = \sqrt{(1)^2 + (-j)^2} = \sqrt{2}$$

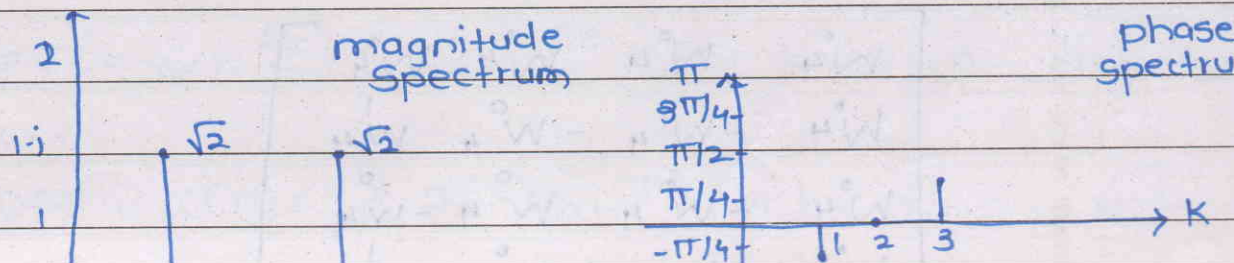
$$0 = 0$$

$$1+j = \sqrt{(1)^2 + (j)^2} = \sqrt{2}$$

$$|x(k)| = \{2, \sqrt{2}, 0, \sqrt{2}\}$$

$$\angle x(k) = \tan^{-1} \left( \frac{\text{Im}}{\text{Re}} \right) = \left\{ 0, -\frac{\pi}{4}, 0, \frac{\pi}{4} \right\}$$

05





B]  $x[n] = a^n u[n]$

$$X(j\omega) = \sum_{n=-\infty}^{\infty} x(n) e^{-j\omega n}$$

$$= \sum_{n=0}^{\infty} a^n \cdot 1 e^{-j\omega n}$$

$$= \sum_{n=0}^{\infty} (a \cdot e^{-j\omega})^n$$

$$= \sum_{n=0}^{\infty} e^{-an} \cdot e^{j\omega n}$$

$$= \sum_{n=0}^{\infty} [e^{-(a+j\omega)}]^n$$

$$= \frac{1}{1 - e^{-(a+j\omega)}}$$

03

$$X(j\omega) = \frac{1}{1 - a \cdot e^{-j\omega}} ; |a \cdot e^{-j\omega}| < 1$$

D]  $x(n) = \{0, 1, 2, 3\}$

$N = 4$

$$X_N = \begin{matrix} & & \begin{matrix} 0 & 1 & 2 & 3 \end{matrix} \\ \begin{matrix} x(0) \\ x(1) \\ x(2) \\ x(3) \end{matrix} & \begin{matrix} 0 \\ 1 \\ 2 \\ 3 \end{matrix} & \begin{bmatrix} W_4^0 & W_4^0 & W_4^0 & W_4^0 \\ W_4^0 & W_4^1 & W_4^2 & W_4^3 \\ W_4^0 & W_4^2 & W_4^4 & W_4^6 \\ W_4^0 & W_4^3 & W_4^6 & W_4^9 \end{bmatrix} \end{matrix} \begin{matrix} x_n \\ x(0) \\ x(1) \\ x(2) \\ x(3) \end{matrix}$$

By using twiddle factor matrix becomes

$$\begin{bmatrix} W_4^0 & W_4^0 & W_4^0 & W_4^0 \\ W_4^0 & -W_4^1 & -W_4^2 & W_4^3 \\ W_4^0 & -W_4^0 & W_4^0 & -W_4^1 \\ W_4^0 & -W_4^1 & W_4^2 & -W_4^3 \end{bmatrix}$$

$$W_N^0 = \left( e^{-j2\frac{\pi}{N}n} \right)^0 = e^0 = 1$$

$$W_4^1 = \left( e^{-j2\frac{\pi}{4}n} \right)^1 = e^{-j\frac{\pi}{2}} = \cos\frac{\pi}{2} - j\sin\frac{\pi}{2} = 0 - j = -j$$

$$W_4^2 = \left( e^{-j2\frac{\pi}{4}n} \right)^2 = e^{-j\pi} = \cos\pi - j\sin\pi = -1 - j(0) = -1$$

$$W_4^3 = \left( e^{-j2\frac{\pi}{4}n} \right)^3 = e^{-j\frac{3\pi}{2}} = \cos\frac{3\pi}{2} - j\sin\frac{3\pi}{2} = 0 - j(-1) = j$$

$$W_4^4 = \left( e^{-j2\frac{\pi}{4}n} \right)^4 = e^{-j2\pi} = \cos 2\pi - j\sin 2\pi = 1 - 0 = 1$$

$$W_4^6 = \left( e^{-j2\frac{\pi}{4}n} \right)^6 = e^{-j3\pi} = \cos 3\pi - j\sin 3\pi = -1 - j(0) = -1$$

$$W_4^9 = \left( e^{-j2\frac{\pi}{4}n} \right)^9 = e^{-j\frac{9\pi}{2}} = \cos\frac{9\pi}{2} - j\sin\frac{9\pi}{2} = 0 - (j) = -j$$

$$X_N = W_N x_n$$

$$\begin{bmatrix} x(0) \\ x(1) \\ x(2) \\ x(3) \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & -j & -1 & j \\ 1 & -1 & 1 & -1 \\ 1 & j & -1 & -j \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \end{bmatrix}$$

$$x(0) = 0 + 1 + 2 + 3 = 6$$

$$x(1) = 0 + (-j) + (-2) + 3j = -2 - 2j$$

$$x(2) = 0 + (-1) + (2) + (-3) = -2$$

$$x(3) = 0 + j + (-2) + (-3j) = -2 + 3j$$

$$x(k) = \{6, -2 - 2j, -2, -2 + 3j\}$$

Twiddle factor :

Twiddle factor are set of values that are used in fast fourier transform to speed up the operations of DTF & IDTF

$$\text{It is denoted as } W_N^{nk} = e^{-j2\frac{\pi}{N}nk}$$

$$\text{DFT} = X(k) = \sum_{n=0}^{N-1} x(n) W_N^{nk} \quad \text{for } k=0, 1, 2, \dots, N-1$$



## Properties of twiddle factor:

① Periodicity Property:  $W_N^{nkN} = W_N^{nk}$

where  $N$  is a complete periodic cycle.

$N = 8$  then

$$W_8^8 = W_8^{16} = W_8^{24} = 1$$

② Symmetric Property:  $W_N^{\frac{nkN}{2}} = W_N^k$

If  $N = 8$  then the values are symmetric in that periodic cycle.

$$W_8^0 = 1 \quad W_8^4 = -1$$

$$W_8^1 = \frac{1}{\sqrt{2}} - j \frac{1}{\sqrt{2}} \quad ; \quad W_8^5 = \frac{-1}{\sqrt{2}} + j \frac{1}{\sqrt{2}}$$





ASHOKRAO MANE GROUP OF INSTITUTIONS, VATHAR.

Faculty of Engineering

## CIRCULAR/NOTICE

Doc. No.: AMGOI-FRM-03

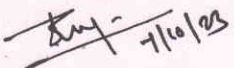
Rev. No.: 00

Rev. Dt: 04/07/2013

Date-07/10/2023

All the students are hereby informed that, departmental MSE Semester Exam is scheduled from **11/10/2023** to **13/10/2023** of **20 marks**. The details of the schedule are as follows.

DATE	TIME	SY	TY	B. Tech
11/10/2023	10.15.am to 11.15 am	EMI	DSP	FOC
11/10/2023	03.00pm to 04.00pm	EDC	AC	ME
12/10/2023	10.15.am to 11.15 am	M III	ACOM	MCOM
12/ 10/2023	03.00pm to 04.00pm	DE	EFT	ED
13/ 10/2023	10.15.am to 11.15 am		CSE	EEFM

  
Mr. S. A. Bhosale  
Exam coordinator

  
Mrs. S. S. Patil  
H.O.D

HOD

Electronics & Telecommunication Engg.  
Ashokrao Mane Group of Institutions  
Vathar Tarf Vadagaon.



**DR. BABASAHEBAMBEDKAR TECHNOLOGICAL UNIVERSITY, LONERE**  
**Mid Semester Examination-Marking scheme with solution—Oct., 2023**

Course: **B. Tech in Electronics & Telecommunication Engineering**      Sem: **V**  
 Subject Name: **Digital Signal Processing**      Subject Code: **BTETC502**  
 Max Marks: **20**      Date: **11/ 10 /2023**      Duration: **1 Hr.**

		(Level/CO)	Marks
<b>Q. 1</b>	<b>Fill in the blank</b>		<b>05*01M</b>
A.	How many complex multiplications are need to be performed for each FFT algorithm? a) $(N/2)\log N$ b) $N \log_2 N$ c) $(N/2)\log_2 N$ d) $N^2$	U/BTETC502.2	01
B.	How many no. of stages required to compute 16 point DFT using DIF FFT algorithm. a) 2      b) 3      c) 4      d) 8	U/BTETC502.2	01
C.	For a decimation-in-time FFT algorithm, which of the following is true? a) Both input and output are in order b) Both input and output are shuffled c) <b>Input is shuffled and output is in order</b> d) Input is in order and output is shuffled	U/BTETC502.2	01
D.	4-point DFT of a real time discrete signal $x[n]$ of length 4 is given by $X(k)$ ; $k = 0, 1, 2, 3$ . It is given that $X(0) = 5$ ; $X(1) = 1 + j1$ ; $X(2) = 0.5$ & $X(3) =$ _____ a) -0.5    b) -1-j1    c) <b>1-j1</b> d) -5	A/BTETC502.2	01
E.	Multiplying sequence $x(n)$ by $e^{j\omega_0 n}$ in time domain corresponds to frequency shift by ' $\omega_0$ ' in frequency domain this is called as a) Time shifting property      b) Periodicity Property c) <b>Frequency shifting property</b> d) Correlation theorem	U/BTETC502.2	01
<b>Q.2</b>	<b>Solve any Three of the following.</b>		<b>03*05 M</b>
A.	Determine Output response $y(n)$ if $h(n) = \{1, 1, 1\}$ and $x(n) = \{1, 2, 3, 4\}$ by using i) Circular convolution    ii) circular convolution using linear convolution. Write comment on result.  <b>Ans:</b> i) $y(n) = \{8, 7, 6, 9\}$ ----- (2M) ii) $y(n) = \{1, 3, 6, 9, 7, 4\}$ ---- (2M) <b>comment:</b> In circular convolution first 2 points are result of overlapping of first and last 2 points from linear convolution i.e In circular convolution aliasing effect takes place. ----- (1M)	A/BTETC502.2	05
B.	Explain any four properties of DFT. Each property statement & proof ----- (1.25M)	U/BTETC502.2	05
C.	Compute the FFT of a sequence $x(n) = n+1$ where $N=4$ using 'Decimation in Time' algorithm. <b>Ans:</b> 1 <sup>st</sup> stage calculations and flow diagram ----- (2M) 2 <sup>nd</sup> stage calculations and flow diagram----- (2M) $X(k) = \{10, -2+2j, -2, -2-2j\}$ ----- (1M)	A/BTETC502.2	05
D.	Compute the FFT of a sequence $x(n) = \{1, -1, 1, -1\}$ where $N=4$ using 'Decimation in Frequency' algorithm. <b>Ans:</b> 1 <sup>st</sup> stage calculations and flow diagram ----- (2M) 2 <sup>nd</sup> stage calculations and flow diagram----- (2M) $X(k) = \{0, 0, 4, 0\}$ ----- (1M)	A/BTETC502.2	05



Shri Balasaheb Mane Shikshan Prasarak Mandal, Ambap's  
Ashokrao Mane Group of Institutions, Faculty of Engineering  
Vathar Tarf Vadgaon- 416112

Exam: Mid Sem

Branch: E&TC Engg.

Time: 10:30 to 11:30

Subject: Digital signal processing Date: 11/10/2023

Roll No.	Name of student	Sign	Marks( )
01	Bhosale Dhairyashil Pratap	<u>Dhairyashil</u>	04+05=09
02	Chougule Suyog Rajkumar	<u>SChougule</u>	03+05=08
03	Pandurang Namadev Gopane	<u>Gopane</u>	05+08=13
04	Geeta Chandrakant Jagtap	<u>Jagtap</u>	04+11=15
05	Rushikesh Ramesh Kumbhar	<u>Kumbhar</u>	04+10=14
06	Sakshi Sachin Lambe	<u>Lambe</u>	04+11=15
07	Shreyansh Sunil Kininge	<u>Kininge</u>	04+07=11
08	Diksha D. Mane	<u>D. Mane</u>	05+13=18
09	Sakshi A. Mutnale	<u>Mutnale</u>	05+11=16
10	Aditi Raosaheb Patil	<u>APatil</u>	04+12=16
11	Patil Akshay Dilip	<u>A. D. Patil</u>	05+05=10
12	Aniket Vishwanath Patil	<u>Patil</u>	04+08=12
13	AYUSH Subhash Patil	<u>Patil</u>	04+07=11
14	Ketan Krushnat Patil	<u>K.K.Patil</u>	04+06=10
15	Pratik Dattatray Patil	<u>Patil</u>	04+06=10
16	Rohan Shivaji Patil	<u>Patil</u>	05+05=10
17	Rohini Bharama Patil	<u>Patil</u>	04+10=14
18	Sakshi Madhukar Patil	<u>SPatil</u>	04+10=14
19	Vaushabh Babaso Patil	<u>Patil</u>	04+04=08
20	Peanita Shekhar Poware	<u>Peanita</u>	03+11=14
21	Poojakumari N. Rajput	<u>P. Rajput</u>	03+12=15
22	Sanamkumari N. Rajput	<u>Sanam</u>	03+10=13
23	Ritesh Shashikant Patil	<u>R. Patil</u>	04+10=14
24	Arati Ramchandra Salunke	<u>Salunke</u>	04+14=18
25	Shubham Manali Shinde	<u>Shinde</u>	00+08=08
26	Shirish. Y. Shipekar	<u>Shirish</u>	05+07=12
27	Kajal Mahadev Shirke	<u>Shirke</u>	05+10=15
28	Vaishnavi Vishwas Yadav-Patil	<u>V. Patil</u>	04+10=14
29	Prachi Raghunath Yadav	<u>P. Yadav</u>	05+11=16
30	Suyash Sanjay Desai	<u>Desai</u>	03+10=13
31	Pooja M. Poware	<u>P. Poware</u>	04+14=18
32	Saarthak Sachin Jadhav	<u>S. Jadhav</u>	03+07=10

Total No. of Present Student: 36

Total No. of Absent Student: 01

Total No. of Student: 37

D. Mali  
Jr. Supervisor Name & Sign



**Shri Balasaheb Mane Shikshan Prasarak Mandal, Ambap's  
Ashokrao Mane Group of Institutions, Faculty of Engineering  
Vathar Tarf Vadgaon- 416112**

Exam: Mid sem

Branch: E&TC Engg.

Time: 10:30 to 11:30

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Date: 11/10/2023

Roll No.	Name of student	Sign	Marks( )
33	Shriya R. Wayangankar	<u>[Signature]</u>	04+12=16
34	Manasi Sannaki	<u>mgs</u>	04+12=16
35	Anjali Patil	<u>[Signature]</u>	03+09=12
36	snheet. chougule.	<u>[Signature]</u>	03+06=09
37	Pathan Umar		
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Q.2 c)  $x(n) = n+1 \quad N=4$

$\therefore x(n) = \{1, 2, 3, 4\}$

DIT-FFT

- Bit Reversal

$00 \rightarrow 00 \quad x(0) = 1$

$01 \rightarrow 10 \quad x(2) = 3$

$10 \rightarrow 01 \quad x(1) = 2$

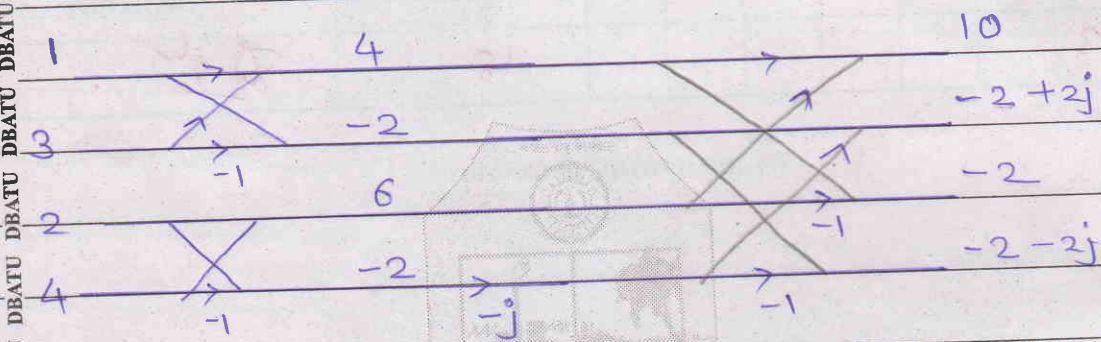
$11 \rightarrow 11 \quad x(3) = 4$

05

show calculation of each stage along with twiddle factor

we get,

$\therefore X(k) = \{10, -2+2j, -2, -2-2j\}$

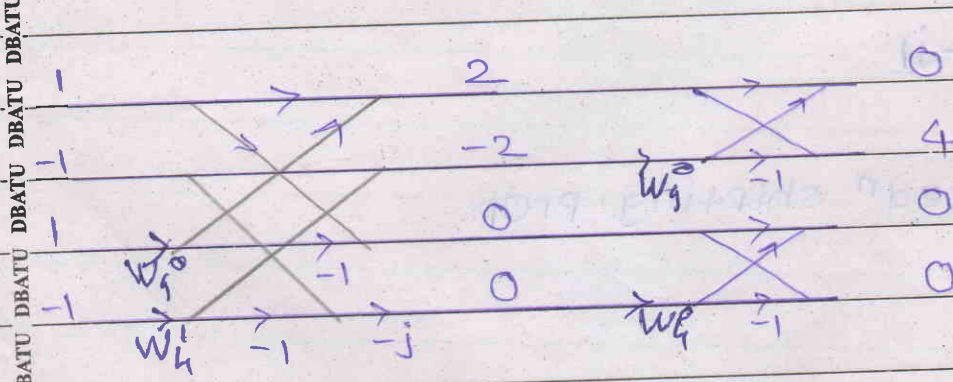


Q.2 d)  $x(n) = \{1, -1, 1, -1\} \quad N=4$

DIF-FFT

04

$\therefore X(k) = \{0, 4, 0, 0\}$





Q.2

A.

$x(n) = \{1, 2, 3, 4\}$   $h(n) = \{1, 1, 1\}$   $h(n) = \{1, 1, 1, 0\}$

$y(n) = x(n) * h(n) = \sum_{k=0}^{N-1} x(k) \cdot h(n-k)$

i) circular convolution:

$$[y_n] = \begin{bmatrix} 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix}$$

$$y_n = \begin{bmatrix} 1+0+3+4 \\ 1+2+0+4 \\ 1+2+3+0 \\ 0+2+3+4 \end{bmatrix}$$

$$\therefore \begin{bmatrix} y(0) \\ y(1) \\ y(2) \\ y(3) \end{bmatrix} = \begin{bmatrix} 8 \\ 7 \\ 6 \\ 9 \end{bmatrix}$$

$\therefore y(n) = \{8, 7, 6, 9\}$

ii) circular convolution using linear convolution

- Linear

$x(n)$	1	2	3	4
$h(n)$	1	2	3	4
	1	2	3	4
	1	2	3	4
	1	2	3	4

$\therefore y(n) = \{1, 3, 6, 9, 7, 4\}$

Length of  $x(n)$   $L = 4$

length of  $h(n)$   $M = 3$

$\therefore$  Length of  $y(n) = L + M - 1 = 4 + 3 - 1 = 6$

• circular convolution using Linear

$\therefore$  padding zeros

$x(n) = \{1, 2, 3, 4, 0, 0\}$

$h(n) = \{1, 1, 1, 0, 0, 0\}$

~~$y_n =$~~

1	0	0	1	1	1
1	1	0	0	1	1
1	1	1	0	0	1
0	1	1	1	0	0
0	0	1	1	1	0

$y_n =$

1	0	0	0	1	1	1
1	1	0	0	0	1	2
1	1	1	0	0	0	3
0	1	1	1	0	0	4
0	0	1	1	1	0	0
0	0	0	1	1	1	0

$y_n =$

1 + 0 + 0 + 0 + 0 + 0
1 + 2 + 0 + 0 + 0 + 0
1 + 2 + 3 + 0







ASHOKRAO MANE GROUP OF INSTITUTIONS, VATHAR.  
Faculty of Engineering

## CIRCULAR/NOTICE

Doc. No.: AMGOI -FRM-03

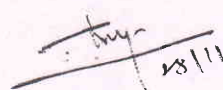
Rev. No.: 00


Rev. Dt: 04/07/2013

Date-28/11/2023

All the students are hereby informed that, departmental CA-II Semester Exam is scheduled from 01/12/2023 to 02/12/2023 of 20 marks. The details of the schedule are as follows.

DATE	TIME	SY	TY	B.Tech
01/12/2023	10.15.am to 11.15am	M-III	EFT	FOC
01/12/2023	12.30pm to 01.30pm	EDC	DSP	ED
01/12/2023	02.30pm to 03.30pm	-	ACOM	MCOM
02/ 12/2023	10.15.am to 11.15am	DE	AC	ME
02/ 12/2023	12.30pm to 01.30pm	EMI	CSE	EEFM

  
Mr. S. A. Bhosale  
Exam coordinator

  
Mrs. S. S. Patil  
H.O.D  
HOD

Electronics & Telecommunication Engg.  
Ashokrao Mane Group of Institutions  
Vathar Tarf Vadagaon.





**DR. BABASAHEBAMBEDKAR TECHNOLOGICAL UNIVERSITY, LONERE**  
**Continuous Assessment-II DEC., 2023**

Course: **B. Tech in Electronics & Telecommunication Engineering**      Sem: **V**  
 Subject Name: **Digital Signal Processing**      Subject Code: **BTETC502**  
 Max Marks: **20**      Date: **01/11/2023**      Duration: **1 Hr.**

**Instructions to the Students:**

1. Solve all questions .
2. Assume suitable data if required.
3. Use of non-programmable scientific calculator is allowed.

		(Level/CO)	Marks
<b>Q. 1</b>	<b>Fill in the blank</b>		<b>05*01M</b>
<b>A.</b>	The magnitude response of Butterworth filter has a) Flat pass band and Flat stop band b) Flat pass band and Tapering stop band c) Tapering pass band and Flat stop band d) Tapering pass band and Tapering stop band	R/BTETC502.6	<b>01</b>
<b>B.</b>	The transformation technique in which there is one to one mapping from s-domain to z-domain is ___ a) Approximation of derivatives      b) Impulse invariance method c) Bilinear transformation method      d) Backward difference for the derivative	R/BTETC502.6	<b>01</b>
<b>C.</b>	Stable poles from s- plane maps- a) Inside unit circle in z-plane      b) Outside unit circle in z-plane c) On unit circle in z-plane      d) None of the above	U/BTETC502.6	<b>01</b>
<b>D.</b>	Consider the assertions given below. Which among them is an advantage of FIR Filter? a) Necessity of computational techniques for filter implementation b) Requirement of large storage c) Incapability of simulating prototype analog filters d) Presence of linear phase response	R/BTETC502.6	<b>01</b>
<b>E.</b>	In FIR filter design, which among the following parameters is/are separately controlled by using Kaiser window? a) Order of filter      b) Transition width of main lobe c) Both a) and b)      d) None of the above	R/BTETC502.6	<b>01</b>
<b>Q.2</b>	<b>Solve any Three of the following.</b>		<b>03*05 M</b>
<b>A.</b>	For analog transfer function $H(s) = 1/s^2 + 3s + 2$ , Determine $H(z)$ using impulse invariant technique.	A/BTETC502.3	<b>05</b>
<b>B.</b>	What is bilinear transformation? Explain frequency warping effect & prewarping procedure in BLT method.	U/BTETC502.3	<b>05</b>
<b>C.</b>	Design the second order low pass digital Butterworth filter with following specifications, Cutoff frequency=1KHz Sampling frequency=104 sps $H(s) = 1/s^2 + \sqrt{2} s + 1$	A/BTETC502.3	<b>05</b>
<b>D.</b>	Obtain following realizations of system functions: i) $H(z) = (1 + 2z^{-1} - z^{-2})(1 + z^{-1} - z^{-2})$ --cascade realization ii) $y(n) = 2r \cos \omega_0 y(n-1) - r^2 y(n-2) + x(n) - r \cos \omega_0 x(n-1)$ —direct form-I	A/BTETC502.6	<b>05</b>

**DR. BABASAHEBAMBEDKAR TECHNOLOGICAL UNIVERSITY, LONERE**  
**Continuous Assessment-II DEC., 2023**

Course: **B. Tech in Electronics & Telecommunication Engineering**

Sem: **V**

Subject Name: **Digital Signal Processing**

Subject Code: **BTETC502**

Max Marks: **20**

Date: **01/11/2023**

Duration: **1 Hr.**

		(Level/CO)	Marks
<b>Q. 1</b>	<b>Fill in the blank</b>		<b>05*01M</b>
<b>A.</b>	The magnitude response of Butterworth filter has a) Flat pass band and Flat stop band <b>b) Flat pass band and Tapering stop band</b> c) Tapering pass band and Flat stop band d) Tapering pass band and Tapering stop band	R/BTETC502.6	<b>01</b>
<b>B.</b>	The transformation technique in which there is one to one mapping from s-domain to z-domain is__ a) Approximation of derivatives      b) Impulse invariance method <b>c) Bilinear transformation method</b> d) Backward difference for the derivative	R/BTETC502.6	<b>01</b>
<b>C.</b>	Stable poles from s- plane maps- <b>a) Inside unit circle in z-plane</b> b) Outside unit circle in z-plane c) On unit circle in z-plane      d) None of the above	U/BTETC502.6	<b>01</b>
<b>D.</b>	Consider the assertions given below. Which among them is an advantage of FIR Filter? a) Necessity of computational techniques for filter implementation b) Requirement of large storage c) Incapability of simulating prototype analog filters <b>d) Presence of linear phase response</b>	R/BTETC502.6	<b>01</b>
<b>E.</b>	In FIR filter design, which among the following parameters is/are separately controlled by using Kaiser window? a) Order of filter      b) Transition width of main lobe <b>c) Both a) and b)</b> d) None of the above	R/BTETC502.6	<b>01</b>
<b>Q.2</b>	Solve <b>any Three</b> of the following.		<b>03*05 M</b>
<b>A.</b>	For analog transfer function $H(s) = 1/s^2 + 3s + 2$ , Determine $H(z)$ using impulse invariant technique.	A/BTETC502.3	<b>05</b>



**Solution**

Given that,  $H(s) = \frac{2}{s^2 + 3s + 2} = \frac{2}{(s+1)(s+2)}$

By partial fraction expansion technique we can write,

$$H(s) = \frac{2}{(s+1)(s+2)} = \frac{A}{s+1} + \frac{B}{s+2}$$

$$A = \frac{2}{(s+1)(s+2)} \times (s+1) \Big|_{s=-1} = \frac{2}{-1+2} = 2$$

$$B = \frac{2}{(s+1)(s+2)} \times (s+2) \Big|_{s=-2} = \frac{2}{-2+1} = -2$$

The roots of quadratic

$$s^2 + 3s + 2 = 0 \text{ are,}$$

$$s = \frac{-3 \pm \sqrt{3^2 - 4 \times 2}}{2}$$

$$= \frac{-3 \pm 1}{2} = -1, -2$$

---(2M)

$$\therefore H(s) = \frac{2}{s+1} - \frac{2}{s+2}$$

By impulse invariant transformation we know that,

$$\frac{A_i}{s+p_i} \xrightarrow{\text{is transformed to}} \frac{A_i}{1-e^{-p_i T} z^{-1}}$$

$$\therefore H(z) = \frac{2}{1-e^{-p_1 T} z^{-1}} + \frac{-2}{1-e^{-p_2 T} z^{-1}} \text{ where } p_1 = 1 \text{ and } p_2 = 2$$

$$H(z) = \frac{2}{1-e^{-T} z^{-1}} + \frac{-2}{1-e^{-2T} z^{-1}}$$

When  $T = 1$  second

$$H(z) = \frac{2}{1-e^{-1} z^{-1}} + \frac{-2}{1-e^{-2} z^{-1}}$$

$$H(z) = \frac{2}{1-0.3679z^{-1}} + \frac{-2}{1-0.1353z^{-1}} = \frac{2(1-0.1353z^{-1}) - 2(1-0.3679z^{-1})}{(1-0.3679z^{-1})(1-0.1353z^{-1})}$$

$$= \frac{2 - 0.2706z^{-1} - 2 + 0.7358z^{-1}}{1 - 0.1353z^{-1} - 0.3679z^{-1} + 0.0498z^{-2}} = \frac{0.4652z^{-1}}{1 - 0.5032z^{-1} + 0.0498z^{-2}}$$

---(3M)

B. What is bilinear transformation? Explain frequency warping effect & prewarping procedure in BLT method.

U/BTETC502.3

05

**The Bilinear transformation** is a mapping that transforms the left half of S-plane into the unit circle in the Z-plane only once, thus avoiding aliasing of frequency components.

The mapping from the S-plane to the Z-plane is in bilinear transformation is

$$S = \frac{2}{T} \left( \frac{1-Z^{-1}}{1+Z^{-1}} \right)$$

The mapping is highly non-linear producing frequency, compression at high frequencies. Neither the impulse response nor the phase response of the analog filter is preserved in a digital filter obtained by bilinear transformation ---(2M)

**Frequency warping effect:**

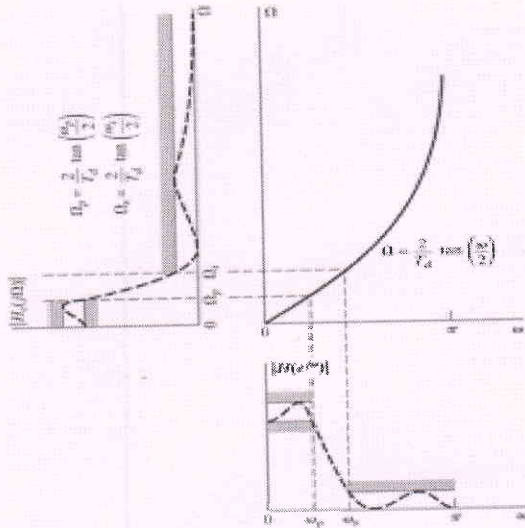
The mapping of frequency from  $\Omega$  to  $\omega$  is approximately linear for small value of  $\Omega$  &  $\omega$ . For the higher frequencies, however the relation between  $\Omega$  &  $\omega$  becomes highly non-linear. This introduces the distortion in the frequency scale of digital filter relative to analog filter. This effect is known as warping effect. ---(1M)

**Prewarping procedure:**

For large frequency values the non linear compression that occurs in the mapping of  $\Omega$  to  $\omega$  is more apparent. This compression causes the transfer function at high  $\Omega$  frequency to be highly distorted when it is translate to the  $\omega$  domain. This compression is being compensated by introducing a prescaling or prewarping to  $\Omega$  frequency scale.

For bilinear transform  $\Omega$  scale is converted into  $\Omega^*$  scale

(i.e)  $\Omega^* = 2/T_s \tan(\Omega T_s/2)$  (prewarped frequency)



we have to account for frequency warping when we start from a discrete-time filter specification.  $\Omega_p = (2/T_s) \tan(\omega_p/2)$  and  $\Omega_s = (2/T_s) \tan(\omega_s/2)$  ---  
**(2M)**

- C. Design the second order low pass digital Butterworth filter with following specifications,  
 Cutoff frequency=1KHz  
 Sampling frequency=104 sps  
 $H(s) = 1/s^2 + \sqrt{2} s + 1$

A/BTETC502.3

05



Shri Balasaheb Mane Shikshan Prasarak Mandal, Ambap's  
Ashokrao Mane Group of Institutions, Faculty of Engineering  
Vathar Tarf Vadgaon- 416112

Exam: CA-II

Branch: E&TC Engg.

Time: 10:35 to 11:15

Subject: Digital Signal Processing (DSP)

Date: 01/12/23

Roll No.	Name of student	Sign	Marks( )
01	Bhosale Dhairyashil Pratap		04+04=08
02	Chougule Suyog Rajkumar		03+05=08
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Total No. of Present Student: 36

Total No. of Absent Student: 01

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Jr. Supervisor Name & Sign

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Ashokrao Mane Group of Institutions, Faculty of Engineering  
Vathar Tarf Vadgaon- 416112**

Exam:

Branch: E&TC Engg.

Time:

Subject:

Date:

Roll No.	Name of student	Sign	Marks( )
33	Shriya Wayangankar	Shriya	05+13=18
34	manasi Sannaki	mgs	05+13=18
35	Anjali Patil	Anjali	05+12=17
36	Sneheet - Chougule	Sneheet	05+05=10
37	Pathan Umar	-	Ab
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Q.2

c)

Given: Cut-off freqn ( $f_c$ ) = 1 kHz

Sampling freqn ( $f_s$ ) =  $10^4$  sps =  $10^4$  Hz

The T.F. of low pass butterworth filter is

$$H(s) = \frac{1}{s^2 + \sqrt{2}s + 1}$$

$$\therefore \omega_c = 2\pi \left( \frac{f_c}{f_s} \right) = 2\pi \left( \frac{1k}{10k} \right)$$

$$= 2\pi(0.1) = 0.2\pi \text{ rad/sec}$$

Pre-warping,

$$\Omega_c = \frac{2}{T} \tan \left( \frac{\omega_c}{2} \right)$$

$$= \frac{2}{1} \tan \left( \frac{0.2\pi}{2} \right) \quad (\because T=1)$$

$$= 2 \tan(0.1\pi)$$

$$\therefore \Omega_c = 0.6109$$

Now, Replace  $s \rightarrow s/\Omega_c$

$$\therefore H_q(s) = \frac{1}{\left( \frac{s}{\Omega_c} \right)^2 + \sqrt{2} \frac{s}{\Omega_c} + 1}$$

$$= \frac{1}{\frac{s^2}{(0.61)^2} + \frac{\sqrt{2}}{0.61} s + 1}$$



$$\therefore H_q(s) = \frac{0.0001}{s^2 + (0.0001)(141.42)s + 0.0001}$$

$$\therefore H_q(s) = \frac{0.0001}{s^2 + 0.014s + 0.0001}$$

To get Butterworth Lowpass filter,

$$\therefore H(z) = H_q(s) \left| s \rightarrow \frac{2}{T} \left( \frac{1-z^{-1}}{1+z^{-1}} \right) \right. \quad T=1$$

$$\therefore H(z) = \frac{0.0001}{\left( \frac{2(1-z^{-1})}{1+z^{-1}} \right)^2 + 0.014 \left( \frac{2(1-z^{-1})}{1+z^{-1}} \right) + 0.0001}$$

is required T.F. of LP Butterworth filter.

Q.2.A

$$H(s) = \frac{1}{s^2 + 3s + 2} = \frac{2s^2}{s^2 + 3s + 2}$$

$$\therefore H(s) = \frac{1}{(s+2)(s+1)}$$

By PFE,

$$H(s) = \frac{1}{(s+2)(s+1)} = \frac{A_1}{s+2} + \frac{A_2}{s+1} \quad \text{--- (1)}$$



$$\therefore A_1 = \frac{1000 \cdot 0}{s+1} = -12 \text{ kHz}$$

$$\& A_2 = \frac{0(s+1)}{(s+2)(s+1)} \Big|_{s=-1}$$

$$\therefore A_2 = 219 \text{ kHz}$$

eqn ① becomes,

$$H(s) = \frac{-1}{s+2} + \frac{1}{s+1}$$

$$\therefore H(s) = \frac{1}{s+1} - \frac{1}{s+2}$$

i.e. in the form,

$$H(s) = \frac{C_1}{s-P_1} + \frac{C_2}{s-P_2}$$

$$\therefore C_1 = 1, C_2 = -1, P_1 = -1, P_2 = -2$$

By impulse invariance technique,

$$H(z) = \sum_{k=1}^N \frac{T \cdot C_k}{1 - e^{P_k T} z^{-1}} \quad T=1$$

$$\therefore H(z) = \frac{1}{1 - e^{-1} z^{-1}} - \frac{1}{1 - e^{-2} z^{-1}}$$



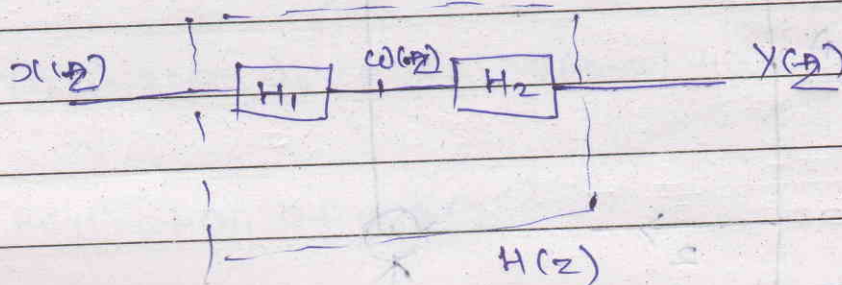
Q.2

D.

$$i) H(z) = (1 + 2z^{-1} - z^{-2})(1 + z^{-1} - z^{-2}) \quad \text{--- (1)}$$

cascade realization.

consider  $H(z) = H_1(z) \cdot H_2(z)$



$$\therefore H_1(z) = \frac{w(z)}{x(z)}$$

$$\therefore 1 + 2z^{-1} - z^{-2} = w(z) \cdot x(z)$$

$$\therefore w(z) = x(z) + 2x(z)z^{-1} - x(z)z^{-2}$$

taking I.Z.T on b.s.

$$\therefore w(n) = x(n) + 2x(n-1) - x(n-2) \quad \text{--- (2)}$$

Now,  $H_2(z) = \frac{Y(z)}{w(z)}$

$$\therefore 1 + z^{-1} - z^{-2} = \frac{Y(z)}{w(z)}$$

$$\therefore Y(z) = w(z) + w(z)z^{-1} - w(z)z^{-2}$$

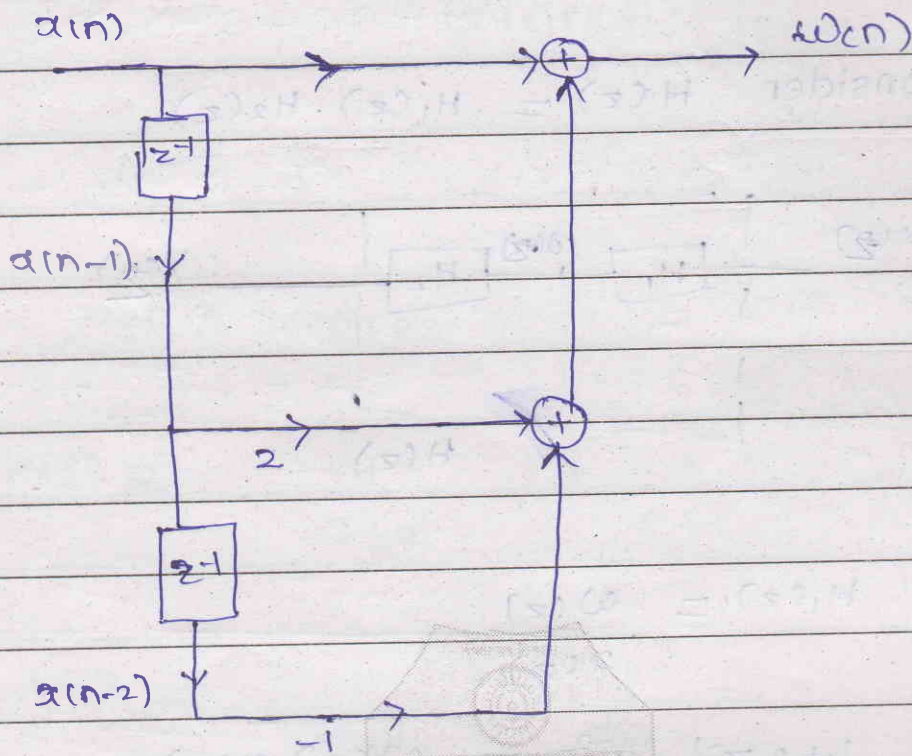
taking I.Z.T on b.s.

$$\therefore y(n) = w(n) + w(n-1) - w(n-2) \quad \text{--- (2)}$$



cascade realization of eqn ① is -

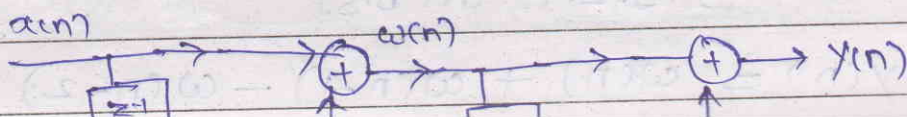
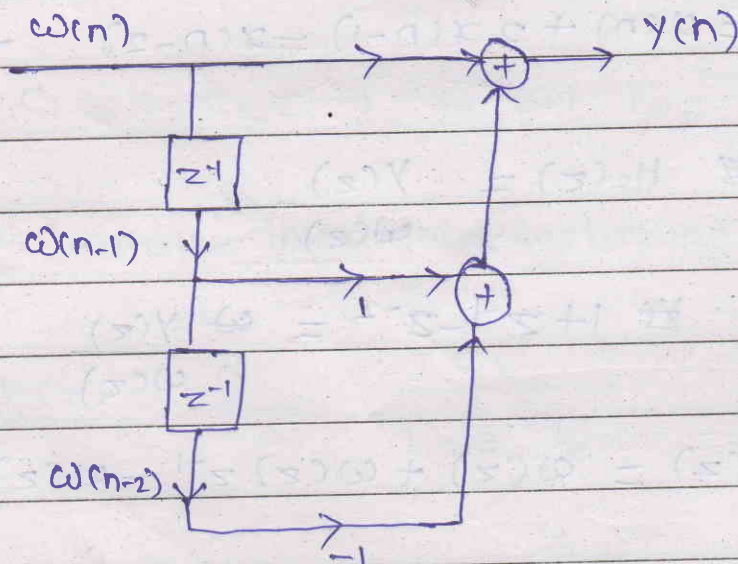
$$w(n) = x(n) + 2x(n-1) - x(n-2)$$



&

cascade realization of eqn ②,

$$y(n) = w(n) + w(n-1) - w(n-2)$$





D.

$$ii) y(n] = 2r \cos \omega_0 y[n-1] - r^2 y[n-2] + x[n] - r \cos \omega_0 x[n-1]$$

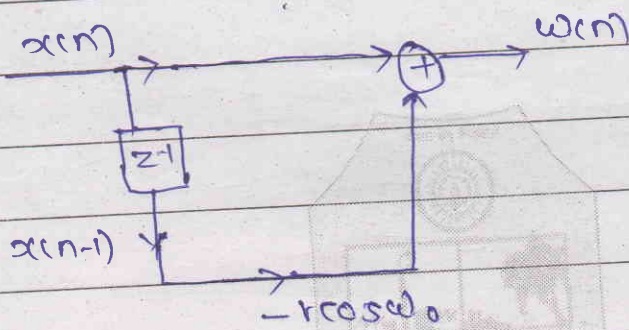
By Direct form-1,

consider,

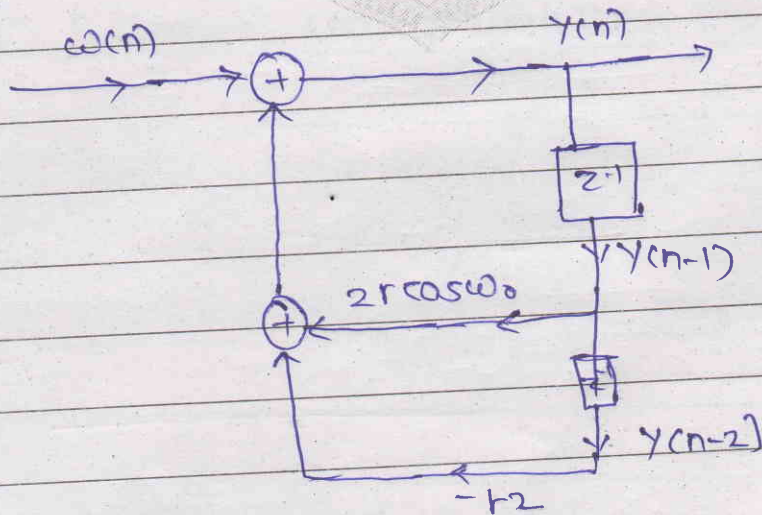
$$w[n] = x[n] - r \cos \omega_0 x[n-1] \quad \text{--- (1)}$$

$$\therefore y[n] = 2r \cos \omega_0 y[n-1] - r^2 y[n-2] + w[n] \quad \text{--- (2)}$$

Realization of eqn (1) is -



Realization of eqn (2),



Realization of eqn ① and ②,

